

Energy-Efficient Resource Allocation in Multicarrier NOMA Systems with Fairness

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Abstract—Non-orthogonal multiple access (NOMA) has attracted both academic and industrial interest since it has been considered as one of the promising 5G technologies in order to increase connectivity and spectral efficiency. In this paper, we focus on a downlink multicarrier (MC) NOMA network, where a single base station serves a set of users through multiple subchannels. The goal is to jointly optimize energy efficiency (EE) and fairness among users with respect to the subcarrier and power allocation parameters. To achieve this with acceptable complexity, a novel greedy subcarrier assignment scheme based on the worst-user first principle is proposed. Due to the fractional form of the EE expression and the existence of interference, the power allocation problem is non-convex and NP-hard. To this end, we first transform this into an equivalent subtractive form, which is then solved by using fractional programming with sequential optimization of the inter/intra-subchannel power allocation vectors. Simulation results reveal the effectiveness of the proposed scheme in terms of EE and fairness among users compared to baseline schemes. Finally, the proposed algorithms are of fast convergence, low complexity, and insensitive to the initial values.

Index Terms—Non-Orthogonal Multiple Access, Successive Interference Cancellation, Quality of service, Energy Efficiency, Power Allocation

I. INTRODUCTION

WITH the explosive growth of the internet-of-things (IoT), and the cloud-based applications, wireless communications require a paradigm shift to support large-scale connectivity and diverse data and latency requirements. To this direction, non-orthogonal multiple access (NOMA) has

attached great interest from both academia and industry [1], due to its superiority in gaining spectral efficiency, mass connectivity and low latency, compared to orthogonal multiple access (OMA). Even though intra-cell interference is increased, NOMA can simultaneously serve multiple users over the power domain (PD), by using the same spectrum band [2]. PD-NOMA uses superposition coding (SC) to broadcast multiple users' message signals by considering the difference of their channel gain conditions. At the receiving end, each user applies successive interference cancellation (SIC) to extract its own signal from the aggregate received signal.

The integration of NOMA in current wireless communication technology creates several challenges, due to multipath transmission, low signal strength, and intra-cell interference [1], [3]. Also, the utilization of the entire bandwidth by all users might be prohibitive in terms of complexity. To this end, NOMA can be combined with OMA schemes in order to design wireless communication schemes with practical value. For example, multicarrier NOMA (MC-NOMA) can be used [1], [2], which enables the simultaneous utilization of a subset of subcarriers from solely a subset of users. Moreover, it is useful to consider an efficient resource allocation technique, which can achieve high transmission rate, low complexity, small latency, and seamless connectivity through network coverage. Furthermore, an effective method for adaptive bandwidth and power allocation is urgently required, in order to avoid the inevitable "spectrum crunch", due to the limited bandwidth and increasing number of users.

A. Related works

Resource allocation for NOMA has been investigated in [4] and [5], where, the primary focus has been on the sum rate maximization under the total power and proportional rate constraints. Furthermore, MC-NOMA was investigated in [6] and [7]. In [6], by considering perfect channel state information (CSI) at the base station (BS), a near optimal solution for power allocation was proposed, while in [7], an efficient power allocation scheme under imperfect CSI for different quality-of-service (QoS) requirements was introduced. In the aforementioned studies, the ultimate goal was to minimize the total transmit power. Besides, joint power allocation and subcarrier assignment for NOMA has been investigated in [9]–[11]. More specifically, a suboptimal joint power and subcarrier allocation was presented in [9], for the maximization of the weighted system throughput. Furthermore, in [10], the authors investigated the optimal power allocation under

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QoS constraints in order to maximize the weighted sum rate and in [11], the authors presented theoretical insights and an algorithm for the sum rate maximization. However, these schemes maximize either the system throughput or the overall sum rate maximization, where user fairness is not considered, which is of crucial criterion in the design on NOMA networks.

Several works have been studied for resource allocation in NOMA to ensure fairness, e.g., [12]–[15]. The power allocation scheme for NOMA networks with α -fairness consideration was studied in [12]. Moreover, the optimal power allocation based on max-min fairness for users on a single channel was investigated in [13] and [14], using statistical CSI and instantaneous CSI, respectively. The authors of [15] exploited the proportional fairness scheduling to maximize the weighted max-min fairness, where the optimal solution was only achieved for two users on a single resource block. It is notable that the aforementioned works in NOMA consider user fairness in terms of achievable rate under the max-min optimization approach. However, no works have been considered on the max-min optimization to ensure fairness of EE among users.

Driven by the rapid growth of data traffic and wireless terminals, energy consumption of wireless networks has been rapidly increasing, and thus energy-efficient design for the next generations of wireless communication system is of paramount importance [45]. To this end, resource allocation scheme which aim to improve the EE has become an important research topic in the design of NOMA networks. For example, in [17], an energy-efficient power allocation strategy in millimeter wave massive MIMO with NOMA has been investigated. In [18], an energy-efficient transmission scheme has been studied for SISO-NOMA systems. Moreover, the joint power allocation and channel assignment for maximizing the EE in NOMA systems was considered in [19]. The same authors in [20] further extended the work in [19] proposing a joint subchannel and power optimization framework for the downlink NOMA heterogeneous network to improve the EE. However, the proposed solution focused solely on improving the overall system's EE, which result in unbalanced use of network resources.

B. Motivation and contribution

The works mentioned above [17]–[20], mainly focus on the improvements of the overall system's EE, which is described as the ratio of sum-rate and the overall energy consumption of all users. The overall EE is a significance performance metric for system design, however, the system mainly benefits from users in better channel conditions or low sever of interference and thus, improvements obtained at the cost of users in the poor channel conditions [40]. Thus, the overall EE causes unfairness among users [40], which is a challenging problem in practical MC-NOMA networks [44]. On the other hand, the EE for each individual user is a particularly useful metric, since it can provide higher performance to the weaker users, while also reducing the utilized energy [16], [33]. Thus, different from the existing works [17]–[20], in this paper, we investigate a fairness based optimization in downlink MC-NOMA systems

to maximize the individual EE which is expressed as the ratio of the user rate to its consumed power (bits/Joule) [16], [22]. For this purpose, we choose the max-min approach to be the objective function, which apart from EE, also preserves fairness among all users in the system [40]. The max-min optimization approach can provide fairness for all users, which is particularly important in networks where some users may have stringent EE requirement.

To the best of our knowledge, the max-min optimization approach to maximize EE while ensuring fairness among users by jointly optimizing the subcarrier and power allocation in MC-NOMA network has not been considered in the open literature. Meanwhile, an energy-efficient resource allocation that considers user's fairness is of vital importance for the next-generation communication systems in order to share resources fairly while maximizing the EE. To this end, this paper investigates for the first time in existing literature the max-min optimization for energy-efficient resource allocation in downlink MC-NOMA systems aiming at improving the EE with fairness. Therefore, in this study, we focus on the most common fairness indication, the max-min EE metric [25], which aims to guarantee fairness for all users by maximizing the minimum EE in the network for the overall available subbands, which motivates the research in this treatise. Moreover, the advantages of this study over the existing works in NOMA is that it refers to MC systems, while it preserves both fairness and energy efficiency.

Furthermore, several iterative algorithms are proposed to solve the problem of EE maximization in NOMA networks, e.g., in single cell NOMA system [19], in NOMA HetNets [20] and for massive MIMO networks in [26]. Although the iterative approach has been applied to various scenarios, the network setting that we consider in this paper is very different, making the existing solutions not directly applicable. For example, if some rules of fairness requirement is strictly imposed in order to guarantee the fairness among all users, the solutions developed in [19], [20], [26] are no longer applicable. To this end, we adopt the SCA techniques to systematically address the critical issue of the inter/intra interference of users in the MC-NOMA networks to maximize users with lowest EE performance. In this setting, we are interested in maximizing the minimum individual EE under the power and minimum rate constraints to optimally allocate the subchannels and transmit power. Moreover, the main contributions of the study are summarized as follows:

- We propose and investigate the maximization of the minimum individual EE under the transmit power and QoS requirements to guarantee fairness among users. The optimization problem of interest is a non-convex problem and, thus, difficult to solve directly due to the fractional structure in the EE expression and the binary variable in the channel allocation indicator. We first decompose the original non-convex problem into two subproblems, namely subchannel assignment and power allocation. As a result, the original problem is solved by a two-stage algorithm that involves approximation and relaxations. We also prove that the max-min EE maximization problem in MC-NOMA is NP-hard with respect to joint subcarrier and power allocation.

- Then, in the first step, we propose a low complexity sub-optimal subcarrier assignment scheme. This is achieved through a greedy algorithm, which incur a reduced computational complexity compared to its exhaustive-searching counterparts.
- Based on the proposed subchannel assignment algorithm, the power allocation subproblem is formulated as a non-convex one due to the existence of the intra-group interference in NOMA networks and the fractional expression in the objective function. Then, by exploiting the property of fractional programming property, the fractional form non-convex optimization is transformed into one of tractable form. Finally, we invoke the framework of sequential successive convex approximation (SCA) [34] to iteratively update the power allocation vector by solving the approximate convex problem. As a result, a low complexity inter/intra subchannel power allocation scheme is proposed, which avoids the high computational complexity of the power optimization problem involving users on the same subcarrier as well as across subcarriers. We also prove the convergence of the proposed algorithm and analyze its complexity in practical MC-NOMA networks.
- Finally, suboptimal power-subcarrier allocation policies are proposed for iteratively improving the EE. Simulations confirm that the MC-NOMA system with the proposed subcarrier assignment and power allocation lead to a considerable performance gain compared to existing works, in terms of both EE and fairness. The proposed scheme achieves near similar performance to the exhaustive-search method at significantly lower computational complexity.

C. Structure

The remaining part of the paper is organized as follows: Section II presents the MC-NOMA system model and problem formulation. In section III, we propose a low complexity greedy based subcarrier assignment scheme. Section IV, presents the fractional programming together with sequential convex programming (SCP) approach to propose an iterative power control algorithm and suboptimal user power allocation scheme to allocate the available power on multiplexed users. Finally, the performance of the proposed method is evaluated in section V by computer simulation, while the paper is concluded in section VI.

II. SYSTEM MODEL AND PROBLEM FORMULATION

In this section, we introduce the system model of the considered downlink MC-NOMA systems, while we also formulate the problem of energy-efficient optimization problem to maximize the minimum users' EE with both subcarrier assignment and power allocation.

A. System Model

A single-cell based downlink MC-NOMA system scenario is considered, where a BS simultaneously transmits information to K users, as illustrated in Fig.1. All transceivers are equipped with a single-antenna. Let P_t denote the total

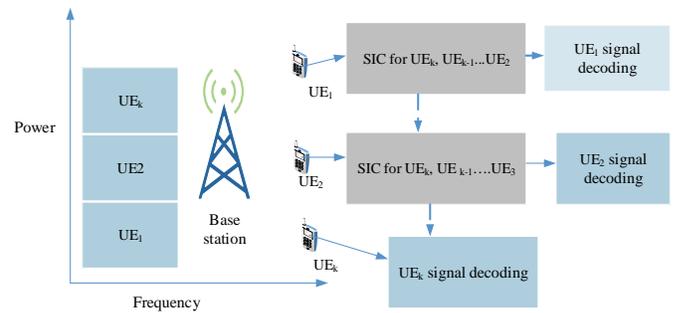


Fig. 1: Downlink NOMA for K users through power domain multiplexing

transmit power. The total available bandwidth B is equally divided into N subcarriers, each with a bandwidth of $W = \frac{B}{N}$. In this paper, the terms subchannel and subcarrier are used interchangeably. In addition, we assume that each user can occupy only S subcarriers and each of the N subcarriers is allocated at most K_n users. The channel between user k and the BS on subcarrier n is denoted by $h_{k,n}$, and we assume that the BS has perfect knowledge of CSI. Based on the CSI of each channel, the BS assigns a subset of subchannels to the users and allocates different levels of power to them. Let $K_n \in \{K_1, K_2, \dots, K_N\}$ be the number of users using subchannel $n = \{1, 2, 3, \dots, N\}$ and $UE_{k,n}$ denotes user k on each subchannel n for $k = \{1, 2, 3, \dots, K_n\}$. Then, the corresponding transmitted signal on each subchannel n is represented by

$$x_n = \sum_{k=1}^{K_n} \sqrt{p_{k,n}} s_k, \quad (1)$$

where s_k is the symbol of $UE_{k,n}$ and $p_{k,n}$ is the power allocated to the k -th user over the n -th subchannel (i.e., $UE_{k,n}$). The received signal at $UE_{k,n}$ is

$$y_{k,n} = \sqrt{p_{k,n}} h_{k,n} s_k + \sum_{i=1, i \neq k}^{K_n} \sqrt{p_{i,n}} h_{i,n} s_i + z_{k,n}, \quad (2)$$

where $h_{k,n} = g_{k,n} d_k^{-\gamma}$ is the channel coefficient from the BS to $UE_{k,n}$ and $g_{k,n}$ is the small scale fading parameter that follows a complex Gaussian distribution, i.e., $g_{k,n} \sim CN(0, 1)$, d_n is the distance between the BS and $UE_{k,n}$, γ is the path loss exponent, and $z_{k,n} \sim CN(0, \alpha_n^2)$ is the additive white Gaussian noise (AWGN).

Using the main principle of power-domain NOMA, multi-user signal separation is conducted at the receiver side using the SIC approach [2]. By exploiting SIC and assuming perfect CSI, the users with better channel conditions can successfully decode the messages of the weaker users. Let $\Upsilon_{k,n} = \frac{|h_{k,n}|^2}{\alpha_n^2}$ denotes the channel response normalized by noise (CRNN) and consider that K_n users are allocated on the n -th subchannel. Without loss of generality, the users at the n -th subchannel are sorted in a descending order as $\Upsilon_{1,n} \geq \dots \geq \Upsilon_{k,n} \dots \geq \Upsilon_{K_n,n}$. Thus, $UE_{1,n}$ is the user which has the best channel conditions on subcarrier n , while $UE_{K_n,n}$ is the user which has the worst channel condition on the same subcarrier on channel n . According to the NOMA

protocol [23], the BS will allocate more power to the weaker users to provide fairness and facilitate the SIC process, which results in $p_{1,n} \leq \dots \leq p_{k,n} \leq \dots \leq p_{K_n,n}$. Note that the first user (the user with the best channel conditions) will cancel interference from all other users, while the last user (K_n) will see interference from all other users when decoding its own message. In general, $UE_{k,n}$ is able to decode signals of $UE_{i,n}$ for $i > k$ and remove them from its own signals, but treats the signals from $UE_{i,n}$ for $i < k$ as interference. Thus, the interference ($I_{k,n}$) experienced by each user on each subcarrier with this decoding order will be [19]

$$I_{k,n} = \sum_{i=1, i \neq k}^{K_n-1} p_{i,n} \Upsilon_{k,n}. \quad (3)$$

Hence, the received signal to the interference plus noise ratio (SINR) of the k -th user on subchannel n is written as

$$SINR_{k,n} = \frac{P_{k,n} |h_{k,n}|^2}{\alpha_n^2 + I_{k,n}} = \frac{P_{k,n} \Upsilon_{k,n}}{1 + \sum_{i=1, i \neq k}^{K_n-1} p_{i,n} \Upsilon_{k,n}}, \quad (4)$$

where $\alpha_n^2 = E[|z_{k,n}|^2]$ is the noise power and $\Upsilon_{k,n} = \frac{|h_{k,n}|^2}{\alpha_n^2}$ represents the channel response normalized by noise of the k -th user. Thus, the data rate of k -th user is [14]

$$R_{k,n} = W \log_2(1 + SINR_{k,n}). \quad (5)$$

Furthermore, let P_n is the power allocated over subchannel n , then the subchannel power budget and BS power constraints can be expressed as

$$\sum_{k \in K}^{K_n} P_{k,n} = P_n, \quad (6)$$

and

$$\sum_{n=1}^N p_n \leq P_t, \quad (7)$$

respectively. Accordingly, as there are K_n users on subchannel n and N subchannels in the system, the data rate on subchannel n and the total sum rate is given by

$$R_n(P_n) = \sum_{n=1}^{K_n} R_{k,n}(P_{k,n}), \quad (8)$$

and

$$R = \sum_{n=1}^N R_n(P_n), \quad (9)$$

respectively. Moreover, the overall power consumed by each user can be expressed as

$$P_{k,n}^T = \zeta P_{k,n} + P_{k,n}^C, \quad (10)$$

where ζ represents the inverse of the power amplifier efficiency, $P_{k,n}^C$ is the additional circuit power consumption of the k -th transmitter. Individual user's EE is defined as the ratio between the data rate and consumed power for each user [36]. This metric becomes particularly important when a balance between these two metrics is desired for all users. Thus, the EE for each user k is defined as [18]

$$E_\eta(P_{k,n}) = \frac{R_{k,n}(P_{k,n})}{P_{k,n}^T(P_{k,n})}. \quad (11)$$

Moreover, in the downlink MC-NOMA, the SIC process is carrying out at the receiver side [21], [29]. This leads to high computational complexity and possibly a delay at the receiver side as the number of users grouped at the same subchannel increases. Thus, to reduce the computational complexity [19], [25], hereinafter, we consider that each user can occupy one subcarrier and only two users can be multiplexed over a particular subchannel. Thus, $K_n = 2$, for $k = 1, 2 \dots K$ and $K = 2N$. In this case, we assume that the CNRs of $UE_{1,n}$ and $UE_{2,n}$ are ordered as $\Upsilon_{1,n} \geq \Upsilon_{2,n}$. Then, the data rate of the strong user U_1 on subchannel n can be written as

$$R_{1,n} = W \log_2(1 + P_{1,n} \Upsilon_{1,n}), \quad (12)$$

Furthermore, as the weak user U_2 does not perform SIC and treats the signal from strong user as noise, then data rate of the weak user on subchannel n can also be expressed as

$$R_{2,n} = W \log_2\left(1 + \frac{P_{2,n} \Upsilon_{2,n}}{P_{1,n} \Upsilon_{2,n} + 1}\right). \quad (13)$$

B. Problem Formulation

In this section, we introduce an optimization problem for downlink MC-NOMA. Thus, given the expression for the individual EE for each user, the optimization problem can be formulated as

$$\begin{aligned} \max_{Q, P} \min_{k=1, \dots, K} E_\eta(Q, P) &= \frac{R_{k,n}(Q, P)}{P_{k,n}^T(Q, P)}, \\ \text{s.t.} \quad C_1: \sum_{n \in N} R_{k,n} &\geq R_k^{\text{req}}, \quad \forall k \in K, \\ C_2: \sum_{n=1}^N P_n &\leq P_t, \\ C_3: \sum_{k=1}^{K_n} q_{k,n} P_{k,n} &\leq P_n, \quad \forall k \in K, \\ C_4: \sum_{k=1}^K q_{k,n} &\leq K_n, \quad \forall n \in N, \\ C_5: P_{k,n} &\geq 0, \quad \forall k, n, \\ C_6: q_{k,n} &\in \{0, 1\}, \quad \forall k, n, \end{aligned} \quad (14)$$

where the set Q with elements $q_{k,n}$ and P with elements $p_{k,n}$ are the subcarrier allocation policy and the power allocation strategy, respectively. Constraint C_1 guarantees that all users meet their minimum QoS requirements, determined by the rate threshold R_k^{req} for each user k . C_2 and C_3 are constraints for the transmission power of the BS and power budget for each subchannel n , respectively. C_4 ensures that one subcarrier can be with at most K_n users. C_5 retains the power allocation variables to non-negative values. C_6 is a subcarrier allocation variable indicator, which becomes 1 if the user k is multiplexed on subcarrier n , and zero otherwise. Note that (14) is a non-convex optimization problem due to the binary constraint in C_5 and the existence of the interference term and fractional expression in the objective function, and also NP-hard problem [40]. In Appendix A, we will prove that the problem is NP-hard. It is thus impossible to find the optimal solution within a polynomial time.

Theorem 1: Problem (14) is an NP-hard problem (i.e., joint subcarrier and power allocation problem to maximize the EE is NP-hard problem).

Proof: See the proof in Appendix A ■

Once an optimization problem is shown to be NP-hard, we no longer insist on having an efficient algorithm that can find its global optimum in polynomial time [48]. Instead, we have to look at high quality approximate solutions or locally optimal solutions of the problem in polynomial time, which is more realistic in practice. Thus, it is useful to transform this into a sequence of linear programs (LPs) and develop a customized low-complexity algorithm. To make the problem tractable, we first relax $q_{k,n}$ from discrete value of 0 or 1 to continuous real numbers that range in $0 \leq q_{k,n} \leq 1, \forall (k,n) \in K \times N$ [43]. This considered as a time sharing factor for subchannel n that user k is assigned during one block of transmission. Now, the optimization problem in (14) can be reformulated as

$$\begin{aligned} \max_{Q,P} \min_{k=1,\dots,K} E_{\eta}(Q,P) &= \frac{R_{k,n}(Q,P)}{P_{k,n}^T(Q,P)} \\ \text{s.t.} \quad &C_1, C_2, C_3, C_4, C_5, \\ &C_6: q_{k,n} \in [0,1], \quad \forall k,n. \end{aligned} \quad (15)$$

Since problem in (15) is still a fractional non-convex program, it is challenging to find an optimal solution. To this end, we next propose a two-stage algorithm, according to which the subchannel and power allocation processes are sequentially performed.

III. ENERGY-EFFICIENT SUBCARRIER ASSIGNMENT SCHEME

In this section, we propose a low complexity greedy based subchannel algorithm by assuming equal power allocation across the subchannels and fractional transmitted power allocation (FTPA) among multiplexed users on each subcarrier. We prefer FTPA, due to its ability to dynamically allocate power considering different channel gains among users with low complexity [19], [31]. In the FTPA scheme, the transmit power of UE_k on subchannel n is assigned based on the channel gains of all the multiplexed users on subchannel n , as described in [19], is given by

$$P_{k,n} = P_n \frac{(H_{k,n})^{-\sigma}}{\sum_{i=1}^{K_n} (H_{i,n})^{-\sigma}}, \quad (16)$$

where H is the channel gain of user k and i on subchannel n and σ ($0 \leq \sigma \leq 1$) is a decay factor. From (14), it can be seen that as σ increases more power is allocated to users with lower channel gain. The procedure of our proposed suboptimal subcarrier allocation scheme for downlink MC-NOMA system is listed in Algorithm 1. The subcarrier allocation scheme aims at assigning the subcarriers to the k -th user, so that $\min_k \in K, n \in N_{\{H_{k,n}\}}$ is maximized. For example, we consider a general channel quality matrix to demonstrate the operation of each algorithm when assigning users on each subcarrier. To this end, we consider a NOMA system which employs $N=4$ subcarriers to support $K=8$ users in order to allocate two users

on the same subcarrier. Moreover, an OFDMA system which employs $N=4$ subcarriers to support $K=4$ users is considered since only one user is assigned for each subcarrier in OFDMA system. We initially consider an OFDMA system. The channel qualities of the 4 users with respect to 4 subcarriers are given in (M1).

users	U ₁	U ₂	U ₃	U ₄
Sc ₁	<u>2.37</u>	3.59	4.61	1.93
Sc ₂	1.09	1.90	0.46	<u>0.05</u>
Sc ₃	0.84	1.39	<u>3.82</u>	1.96
Sc ₄	1.31	<u>6.60</u>	5.22	1.65

(M1)

where the boldface shows the worst channel quality correspond to each user and the underlined numbers are channel qualities of the subcarrier assigned to users. In the case of the greedy algorithm used in [16], users one by one are allocated to subcarriers with the best channel conditions compared to the available options. As a result, user 1 (U₁) chooses best subcarrier from available four options. So, U₁ selects the 1-st (Sc₁) subcarrier. Next, user 2 (U₂) selects the best subcarrier from the remaining three which is subcarrier 4 (Sc₄). Furthermore, user 3 (U₃) is assigned to subcarrier 3 (Sc₃). Under the lack of any other option, the subcarrier with the worst channel quality is assigned to user 4, i.e., subcarrier 2 (Sc₂). Therefore, the allocated subcarriers to the four users by this algorithm are given by Sc₁ = {U₁}, Sc₂ = {U₄}, Sc₃ = {U₃} and Sc₄ = {U₂}. Accordingly, according to this algorithm, Sc₃ is assigned to U₄ which has the poorest channel quality 0.05. Therefore, one of the disadvantages of a greedy-based algorithm used by [16] is that users at the latter stage are left with limited option. Specifically, as it becomes apparent from the example, at the final stage the 2-nd subcarrier is selected to be assigned to U₄, even though the corresponding channel quality of 0.05 is the worst of all. Consequently, the achievable performance will be governed by this worst subcarrier channel quality. That is $\min_k \in K, n \in N \{h_{k,n}\} = 0.05$.

Another important subcarrier allocation algorithm used by [19] is the suboptimal matching for subchannel assignment (SOMSA) algorithm. The main idea of this algorithm is that each user sends a matching request to its most preferred subchannel. However, this subchannel has the permission to accept the user request if this results to the highest EE, otherwise, the request will be rejected. Thus, the algorithm gives priority to users having the best channel qualities. The operation of this algorithm is demonstrated in detail by using the example in (M2). To begin with, subchannels are ordered in decreasing order of their channel gains as {Sc₄, Sc₂, Sc₁, Sc₃} based on their best channel qualities, forming the matrix shown below:

users	U ₁	U ₂	U ₃	U ₄	U ₅	U ₆	U ₇	U ₈
Sc ₄	1.31	<u>6.60</u>	<u>5.22</u>	1.65	2.12	0.59	1.02	0.06
Sc ₂	1.09	1.90	0.46	0.05	<u>4.72</u>	3.64	<u>4.70</u>	2.37
Sc ₁	<u>2.37</u>	3.59	4.61	1.93	1.73	<u>4.34</u>	1.09	2.72
Sc ₃	0.84	1.39	3.82	<u>1.96</u>	1.98	2.47	1.68	<u>1.38</u>

(M2)

According to (M2), the allocated subcarriers to the eight users by SOMSA algorithm are given by Sc₁ = {U₁, U₆}, Sc₂ = {U₅, U₇}, Sc₃ = {U₄, U₈} and Sc₄ = {U₂, U₃}. The worst channel quality of the allocated subcarrier in this case become $\min_k \in K, n \in N_{\{h_{k,n}\}} = 1.38$, which shows

significant improvement compared to greedy algorithm in [16]. Even though SOMSA is capable of achieving better allocation results compared to [16], at the last stage user 8 (U_8) is forced to select 1.38 value. In NOMA systems where the number of users are more than the number of subcarriers and more users are assigned to the same subcarrier, to achieve a better performance, subcarrier allocation in user oriented approach is more preferable, since it helps to avoid the assignment of subcarriers with poor channel quality [8]. Inspired by this observation, in this paper, we introduce the worst-case user first subcarrier allocation (WCUFSA) algorithm. The WCUFSA algorithm is a greedy based algorithm that allows the users with the worst channel quality to select their desired subcarrier first. To this end, users are arranged in ascending order with respect to the worst channel qualities of all users, as given in (M3). Then, the algorithm first finds the worst channel qualities of the unassigned users and then assigns the best subcarrier to the user with the poorest channel value.

users	U_4	U_8	U_3	U_6	U_1	U_7	U_2	U_5
Sc_1	1.93	<u>2.72</u>	4.61	<u>4.34</u>	2.73	1.09	3.59	1.73
Sc_2	0.05	2.37	0.46	3.64	1.09	<u>4.70</u>	1.90	4.72
Sc_3	<u>1.96</u>	1.38	3.82	2.47	0.84	1.68	1.39	<u>1.98</u>
Sc_4	1.65	0.06	<u>5.22</u>	0.59	<u>1.31</u>	1.02	6.60	2.12

(M3)

As shown in the considered example in (M3), U_4 has the worst channel quality at 2-nd subchannel with channel gain value of 0.05. As a result, it is the first user to select the subcarrier with the best channel quality among the available four subcarriers, which corresponds to the value 1.96. Thus, in the first column, which corresponds to the 4-th user, Sc_3 has the best channel quality. Likewise, other assignments are treated in similar manner using the algorithm iteratively till all subcarriers are assigned to all users (i.e., two users per subcarrier bases). Finally, the set of allocated subcarriers becomes $Sc_1 = \{U_6, U_8\}$, $Sc_2 = \{U_2, U_7\}$, $Sc_3 = \{U_4, U_5\}$, and $Sc_4 = \{U_1, U_3\}$. The gain of the weakest channel utilized for transmission when WCUFSA is used becomes $\min_{k \in K, n \in N} \{h_{k,n}\} = 1.98$. It is clear that WCUFSA is capable of yielding the highest achievable performance in assigning better channel quality to assign a subcarrier to users, compared to the greedy algorithm and SOMSA algorithm, demonstrated in (M1) and (M2), respectively. Therefore, WCUFSA algorithm successfully avoids the assignment of channel with low channel quality even in the last stage. As a summary, the WCUFSA subcarrier allocation scheme is presented in Algorithm 1.

IV. ENERGY-EFFICIENT POWER ALLOCATION FOR NOMA SYSTEM

In this section, we focus on power allocation optimization with the aim to further improve the EE of the NOMA network and guarantee the maximum fairness for NOMA users. The performance of NOMA depends on the selection of the user set over a particular subchannel and allocation of power to the multiplexed users on the subchannel [3], [30]. We assume that the users are assigned to different subchannels by using the subcarrier assignment algorithm, proposed in the previous

Algorithm 1 Subcarrier Allocation Algorithm

- 1: Initialize $U^u = K, A = N, R_{k,n} = 0, q_{k,n} = 0, S_i = \emptyset, P_n = \frac{P_t}{N}$
- 2: Construct channel gain $H \equiv |h_{k,n}|_{N \times K}$
- 3: Obtain the minimum channel gain of each user: $H_k^{min} = \min_{k \in K} \{H_{k,n}\}, i \in A, k \in U$. Then the number of worst channel quality arranged in ascending order (i.e from the worst to best) as $H_{i_0,0}^{min} \leq H_{i_1,1}^{min} \leq \dots \leq H_{i_{N-1},N-1}$, where i_0, i_1, \dots, i_{N-1} indicates subcarrier index in A .
- 4: **while** $U^u \neq \emptyset$ **do**
- 5: **for** $k = 1$ to K **do**
 - (a) Find the user with the minimum channel quality: $k = \arg \min_{k \in U} \{H_{k,i}^{min}\}, \forall k \in K$
 - (b) Assign user k with the subcarrier with the best channel quality: $n = \arg \max_{n \in A} \{H_{k,n}\}$
 - (c) Update $S_k = S_k \cup \{k\}$ and remove k from $U^u = U^u - \{k\}$
- 6: **if** $(|S_k|=2)$ **then**, $A = A - \{n\}$
- 7: A set of two users S_k are assigned on every subcarrier n satisfying the maximum EE
- 8: **end if**
- 9: Obtain power allocation for every two users based on their channel gain using FTPA in (16) or Algorithm 4: $P_{k,n} = |S_k| P_n$
- 10: Update user data rate $R_{k,n}$ based on the current subcarrier allocation:
- 11: $R_{k,n} = \log_2 \left(1 + \frac{P_{k,n} \Upsilon_{k,n}}{1 + \sum_{i=1, i \neq k}^{n-1} P_{i,n} \Upsilon_{k,n}} \right)$
- 12: set $EE_{k,n} = \frac{R_{k,n}}{\zeta P_{k,n} + P_{k,n}^C}$
- 13: **end for**
- 14: **until** $U^u = \emptyset$
- 15: **end while**

section. The resulting optimization problem can be expressed as

$$\begin{aligned}
 & \max_P \min_{k=1, \dots, K} E_\eta(Q, P) = \frac{R_{k,n}(Q, P)}{P_{k,n}^T(Q, P)} \\
 & \text{s.t.} \quad C_1: \sum_{n \in N} R_{k,n} \geq R_k^{\text{req}}, \quad \forall k \in K, \\
 & \quad \quad C_2: \sum_{n=1}^N P_n \leq P_t, \\
 & \quad \quad C_3: \sum_{k=1}^K q_{k,n} P_{k,n} \leq P_n, \quad \forall k \in K, \\
 & \quad \quad C_5: P_{k,n} \geq 0, \quad \forall k, n,
 \end{aligned} \tag{17}$$

The optimization problem in (17) is still non-convex due to the fact that the objective function is the ratio of two real-value functions [16], [32], [33]. Thus, in order to obtain an optimal solution, an exhaustive search is required which is generally computationally infeasible. In order to efficiently solve (17), we transform this into the subtractive form, which is more tractable. Thus, we need to introduce the following problem transformation.

Considering the fractional nature of the EE, the main mathematical tool for solving (21) is fractional programming [28], [36]. This principle holds when the numerator and denominator of the EE optimization problem are concave and convex respectively over convex constraint sets [36]. However, the optimization problem that needs to be solved in (21) is non-convex with respect to the transmit power $P_{k,n}$ due to the terms of multiuser interference. Hence, we invoke the framework of sequential successive convex approximation (SCA) [34] to iteratively update the power allocation vector by solving the approximate convex problem.

B. Sequential convex programming (SCP) for P^*

In this subsection, we propose an SCP optimal approach to obtain an energy-efficient power allocation scheme by iteratively solving the given problem. The proposed iterative power allocation scheme for this paper is named as non-orthogonal multiple access-sequential convex programming (NOMA-SCP). The basic idea of SCP is to approximate a non-convex problem by a sequence of convex problems iteratively [34]. In each iteration, all non-convex constraints are replaced by their inner convex approximations [36]. Due to the non-convexity of problem (20), it is hard to solve it directly with polynomial time complexity. To this end, the objective function in (21) can be rearranged into a difference of two concave function with respect to P_k as

$$R_{k,n}(P) - \eta P_{k,n}^T(P) = f_k(P) - g_k(P) \quad (23)$$

where,

$$f_k(P) = \log_2 \sum_{i=1}^N W(1 + P_{k,n} \Upsilon_{k,n}) - \eta_k P_k(P) \quad (24)$$

$$g_k(P) = \log_2 \sum_{i=1, i \neq k}^N (P_{i,n} \Upsilon_{k,n} + \alpha_{k,n}^2) \quad (25)$$

Now, we can equivalently rewrite (20) as

$$\begin{aligned} & \max_P \min_k \{f_k(P) - g_k(P)\} \\ \text{s.t.} & \quad C_1, C_2, C_4. \end{aligned} \quad (26)$$

It is noted that the objective function in (26) is not smooth at each iteration of different minimum of $f_k(P) - g_k(P)$. Thus, we introduce a new variable \mathcal{R} to the optimization problem (26) to transform into a smooth optimization problem. Thus, (26) can be equivalently formulated as

$$\begin{aligned} & \max_{P_n, \mathcal{R}} \mathcal{R} \\ \text{s.t.} & \quad C_1, C_2, C_4 \\ & \quad C_8: \{f_k(P) - g_k(P)\} \geq \mathcal{R}, \forall k. \end{aligned} \quad (27)$$

It is noted that constraint C_8 in (27) is the difference of two concave functions which can be effectively solved by SCP [35]. At step t we can get an iterative power allocation p^t . Thus, we approximate $g_k(P)$ by first-order Taylor expansion at p^t , i.e.,

$$g_k(P^t) + \nabla g_k^T(P^t)(P - P^t), \quad (28)$$

where $\nabla g_k(P)$ is the gradient of $g_k(P)$ at P and is given by

$$\nabla g_k(P) = \frac{m_k}{\sum_{i=1, i \neq k} P_{i,n} \Upsilon_{k,n} + \alpha_{k,n}^2}. \quad (29)$$

In (29) m_k is a K dimensional column vector with $m_k(k)=0$ and $m_k(i) = \frac{g_{k,i}}{\ln 2}, k \neq i$. Moreover, the minimum data rate constraint C_1 can be equivalently written as

$$C'_1: P_{k,n} \Upsilon_{k,n} + (1 - 2^{R_k^{\text{req}}/W}) \left(\sum_{i=1, i \neq k}^{n-1} P_{i,n} \Upsilon_{k,n} + \alpha_{k,n}^2 \right) \geq 0. \quad (30)$$

Combining (28) and (27), we can rewrite (27) as

$$\begin{aligned} & \max_{P_n, \mathcal{R}} \mathcal{R} \\ \text{s.t.} & \quad C'_1, C_2, C_4 \\ & \quad C_8: f_k(P) - [g_k(P^t) + \nabla g_k^T(P^t)(P - P^t)] \geq \mathcal{R}. \end{aligned} \quad (31)$$

After this transformation, (31) is a smooth and standard convex approximation of (20). The local optimal transmit power can be efficiently calculated by solving (31). The algorithm iteratively solves the convex optimization problem in (31). We show the detailed power control algorithm in Algorithm 3.

Theorem 4: (a) The efficient iterative algorithm always converges, and (b) with any feasible initial values, the optimal transmit power converges to a stationary point of (31), i.e., (20).

Proof: See Appendix D. ■

Algorithm 3 Iterative Algorithm Procedure for P_n^*

- 1: Initialize $t = 0$ and maximum tolerance $\epsilon > 0$
 - 2: Set $P^{(0)}$ calculate $E^0 = \min_k [f_k(P^{(0)}) - g_k(P^{(0)})]$
 - 3: **while** $\|E^{(t+1)} - E^{(t)}\| > \epsilon$ **do**
 - 4: Solve (29) to obtain the solution P^* .
 - 5: Set $t = t + 1$, $P^t = P^*$
 - 6: $E^{(t)} = \min(f_k(P^t) - g_k(P^t))$
 - 7: **end while**
-

Once the power, P_n , for each subchannel n is determined, the next step is to allocate power between multiplexed users on the same subchannel based on users' channel gain. According to the optimization in (22), both the strong and weak users have the same minimum data rate requirement. Users' signals will be multiplexed together using assigned powers and transmitted to users so that the total transmitted power per subchannel not to exceed from the allocated power budget, P_n . Furthermore, the transmit power of the weaker channel gain user must be higher than that of the strong channel gain user [2]. Consequently, an important conclusion about the transmission of power for the strong channel gain user in a NOMA can be drawn from [39]. In [39], the maximum power allocation to the strong channel gain user in downlink NOMA must be smaller than $\frac{P_n}{2^{m-1}}$, where m is the number of users grouped at the same subchannel and P_n is the power budget for each subchannel n [39]. Furthermore, according to constraint C_5 in (22), we have $P_{k,n} \geq 0$, $k \in \{1, 2\}, \forall n \in N$. Thus, the power allocated to the strong channel gain user can efficiently exploit in between 0 and $\frac{P_n}{2^{m-1}}$. Based on our analysis, we can apply an efficient bisection search method to realize the

suboptimal solution of power allocation for users grouped at the same subcarrier, as given in Algorithm 4.

Algorithm 4 Energy-Efficient Power Allocation between multiplexed users

- 1: Initialize $P_{1,n}^{min} = 0$, $P_{1,n}^{max} = \frac{P_n}{2^{m-1}}$ and termination precision $\epsilon > 0$
- 2: **repeat**
- 3: set $P_{1,n} = (P_{1,n}^{min} + P_{1,n}^{max})/2$
- 4: set $P_{2,n} = P_n - P_{1,n}$; solve Eq. (5) to obtain $R_{k,n}$
- 5: **if** $\sum_{k \in N} R_{k,n} \leq R_k^{req}$ **then**
- 6: $P_{1,n}^{max} = P_{1,n}$
- 7: **else**
- 8: $P_{1,n}^{min} = P_{1,n}$
- 9: **end if**
- 10: **until** $(P_{1,n}^{max} - P_{1,n}^{min}) \leq \epsilon$
- 11: output $P_{1,n}^* = P_{1,n}$, $P_{2,n}^* = P_n - P_{1,n}^*$

C. Computational Complexity Analysis

In order to get some insights for the computational complexity of the proposed algorithm, we first recall the optimal subcarrier assignment scheme which can be achieved through exhaustive search. Let us recall the K users and N subcarriers (*i.e.*, $K = 2N$) scenario, we need to search $\frac{(2N)!}{2^N}$ combinations. Thus, the complexity of the exhaustive search becomes $\mathcal{O}(\frac{(2N)!}{2^N})$ [19]. In the proposed greedy algorithm, the complexity comes from the sorting and assignment phases. In the sorting phase, the algorithm finds the minimum channel quality of K users and sorts them from the lower to higher value, which requires $(K(K - 1)/2)$ operations. Furthermore, the algorithm starts from users with the worst channel quality and assigns the subcarrier with the highest channel gain, which requires $(2K \ln K)$ operations. Therefore, the proposed subcarrier assignment algorithm requires $(K(K - 1)/2 + 2K \ln K)$ operations, yielding the complexity of $\mathcal{O}(K^2)$. Let L_1 iterations are required to guarantee the error tolerance, ϵ , for the bisection method. Also, let L_2 denotes the number of iterations required for the power allocation algorithms to converge. Thus, the total complexity of the propose schemes is therefore $\mathcal{O}(K^2 + L_1 L_2 KN)$, which shows lower computational complexity compared even with the optimal subcarrier assignment algorithm alone. Thus, the proposed scheme can be implemented in polynomial time.

V. SIMULATION RESULTS

In this part, we present simulation results to evaluate the performance of the proposed schemes, especially in comparison with the baseline schemes in [19] and [16]. We consider a single BS located in the cell center and users are uniformly distributed inside a circular ring with a radius of 300 m. We set the value of path loss exponent γ as 2 [25]. The minimum distance from users to BS is limited 50 m. The bandwidth of the system is set as 5 MHz. As it has already been mentioned, the considered NOMA network system, two

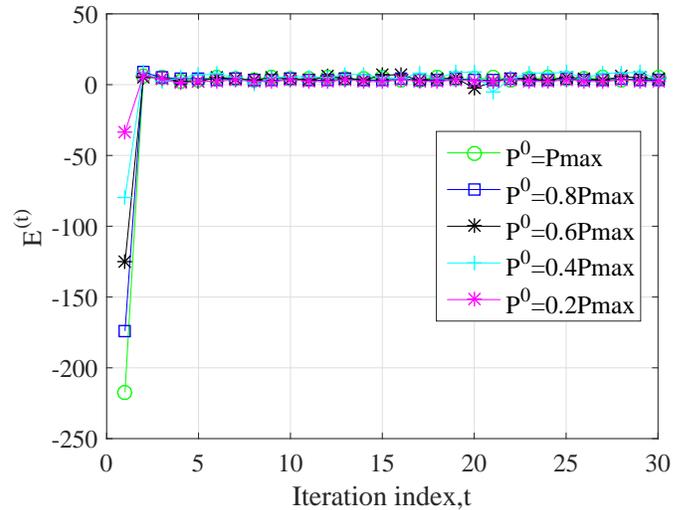


Fig. 2: The convergence of the iterative power allocation algorithm with $\eta^j = 5 \text{ Mbits/joule}$

users are assigned per subcarrier to reduce the complexity of SIC. In the simulation, we set BS peak power $P=12 \text{ W}$, and circuit power consumption $P_c=1 \text{ W}$ [19], and $\alpha_n^2 = \frac{BW * N_0}{N}$, where $N_0=-174 \text{ dBm/Hz}$ is the AWGN power spectral density. For simplicity, we consider each user has the same weighted bandwidth $\frac{BW}{N}$. The performance of the proposed subcarrier assignment (WCUFSA) is compared to suboptimal matching for subchannel assignment algorithm in NOMA (SOMSA) [19] and OFDMA [16]. Regarding the power allocation, the performance of the proposed NOMA-SCP scheme is compared with differential convex programming (NOMA-DC) [19] and OFDMA system as well as NOMA with equal power allocation (NOMA-EQ) used in our proposed subcarrier assignment scheme. Moreover, the proposed user power allocation algorithm (UPA) for users grouped at the same subcarrier is also compared with NOMA-DC-DC [19] and FTPA (fractional transmitted power allocation), which is widely used in NOMA and OFDMA [31].

We first evaluate the feasibility and effectiveness of the proposed algorithms. Fig. 2 and Fig. 3 show the convergence behavior of the efficient iterative power allocation Algorithm and the bisection method for EE (*i.e.*, η^*), respectively. It is noted that both Algorithms converge fast to reach their solution set with different initial transmit power values (*i.e.* P^0). Moreover, the Algorithms reach the solution point within a few iterations. Thus, it is proved that the proposed algorithms can reach to the solution set without being affected by the initial guess power setting. Hence, we can conclude that the proposed algorithms are of high practical value.

In Fig. 4, we compare the proposed subcarrier assignment algorithm (WCUFSA) with SOMSA and OFDMA schemes to evaluate the EE performance for n -th subcarrier as well as the overall EE performance of the whole network. N in the figure denotes the n -th subcarrier. As can be seen in all schemes, they improve the network's EE at the cost of individual EE for the user with the worst channel conditions. However, the proposed algorithm outperforms both SOMSA and OFDMA in terms of

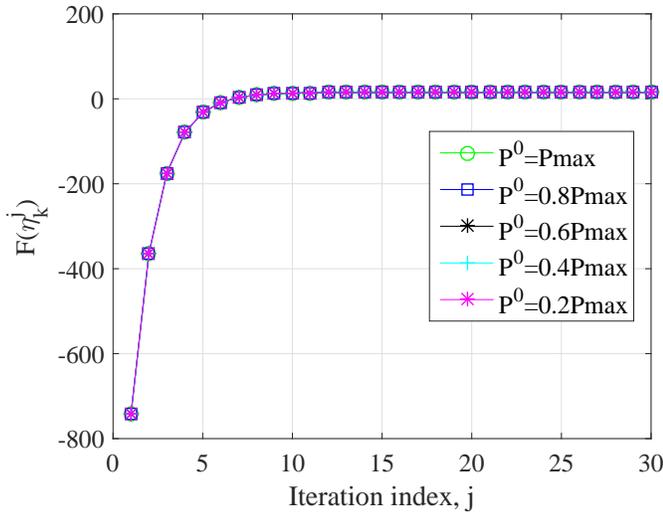


Fig. 3: The convergence of the proposed algorithm 3, the bisection method for maximizing the minimum user’s EE (Max-Min EE)

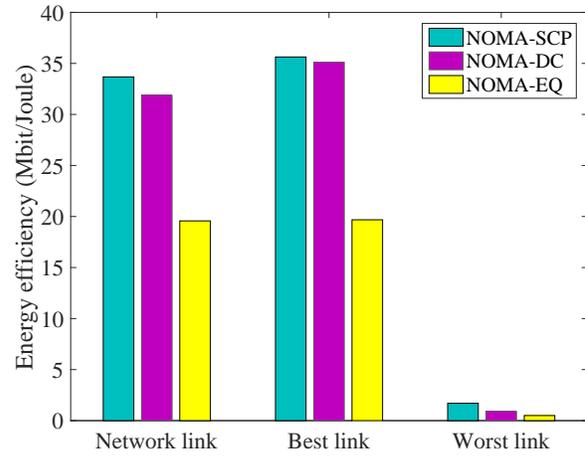


Fig. 5: Comparisons of the EE of the network, the best link, and the worst link among the proposed NOMA-SCP, NOMA-DC, and NOMA-EQ schemes.

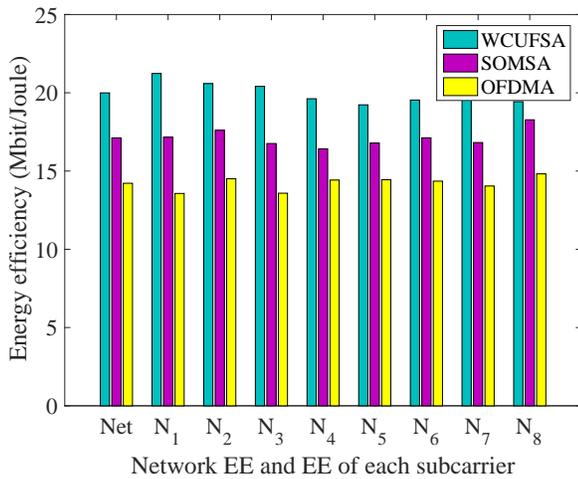


Fig. 4: The EE performance of the network and each subcarrier of three schemes.

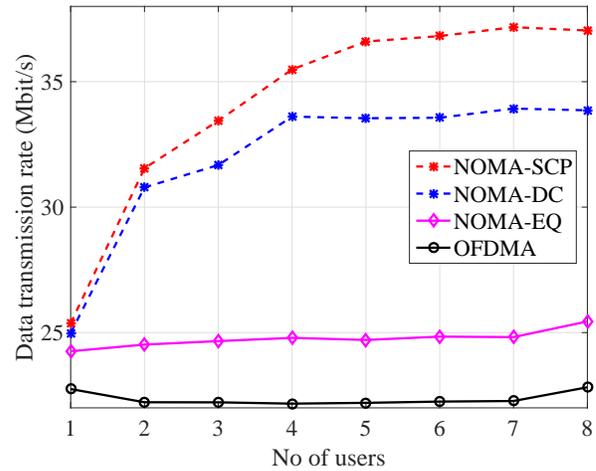


Fig. 6: Data transmission versus number of users

EE as well as fairness among users. In Fig. 5, we further compare the EE performance to evaluate the worst link, the best link, as well as the performance of the network’s EE among the comparable benchmark schemes in terms of EE. It is observed that there is a remarkable difference in the EE among the best link and the worst link in all considered scenarios. However, the EE of NOMA-SCP is well balanced with slightly reduced from network EE as compared to NOMA-DC and NOMA-EQ schemes in a system with 8 subchannels. Fig. 6 shows the achieved data rate of the four schemes against number of users. As it can be seen in Fig. 6, all NOMA schemes are superior to OFDMA schemes in terms of data rate due to the multiplexing gains in NOMA system. Moreover, it also noted that the performance of NOMA-SCP outperforms that of NOMA-DC and NOMA-EQ. As it can be observed from Fig. 6, the data rate of the proposed NOMA-SCP scheme is 6.30% more than that of NOMA-DC in a system with 8 users and

followed by 28.01% and 35.12% more than that of NOMA-EQ and OFDMA scheme, respectively. Therefore, NOMA-SCP can achieve a better data rate transmission performance than that of all comparable schemes. Fig. 7 presents the simulation results for the data transmission performance of different power allocation schemes against transmitted power with the same constraints of Fig. 6. Thus, our proposed power allocation scheme through SCP achieves better performance than the benchmark power allocation scheme.

Fig. 8 presents the simulation results of the EE against the number of K users for different power allocation schemes. We set the precision accuracy as $\epsilon = 0.001$. In the proposed scheme, the achievable EE initially increases fast as the number of users increases and with slow growth rate afterwards. This is due to the multiuser diversity gain by the NOMA system. From Fig. 8, it is shown that the performance of all NOMA schemes are much better than the OFDMA due to the multiplexing gains when NOMA is used. Moreover, it

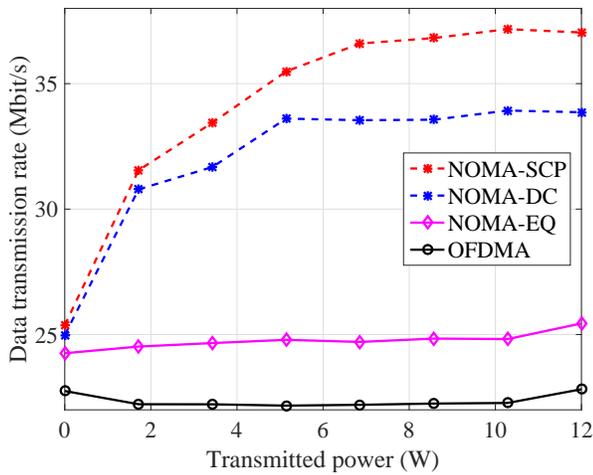


Fig. 7: Data transmission versus transmitted power

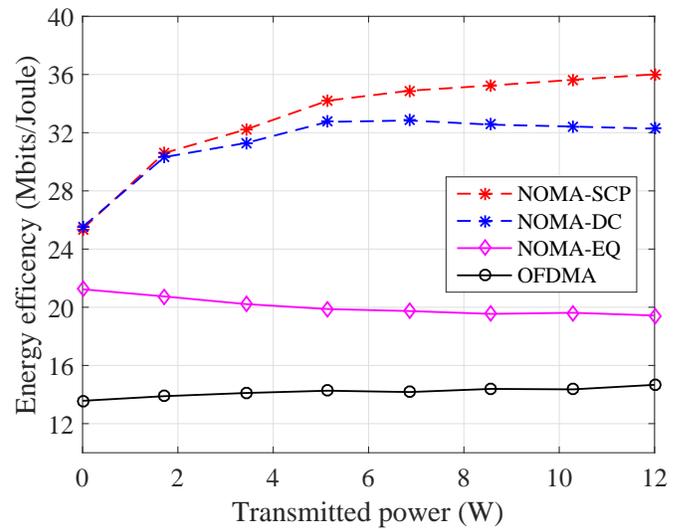


Fig. 9: Energy efficiency versus transmitted power

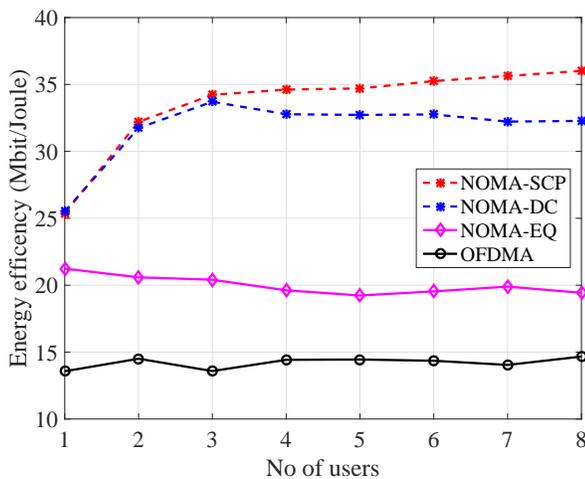


Fig. 8: Energy efficiency versus number of users

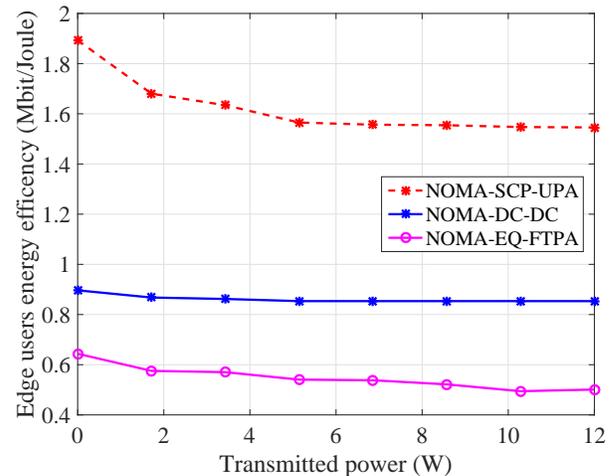


Fig. 10: Edge users EE versus transmitted power

also noted that NOMA-SCP outperforms both NOMA-DC and NOMA-EQ in terms of EE. For example, when the number of user is 8, the EE of NOMA-SCP is 59.21 % more than that of OFDMA scheme. The main reason is that NOMA can support more users in a single subchannel while OFDMA can only support a single user per sub channel. As a result, the BS can not fully utilize spectrum resources as the case of OFDMA system. We also notice that NOMA-SCP improves the EE about 10.38% compared to NOMA-DC. Fig. 9 demonstrates the EE (i.e., η^*) performance versus BS power when fixed circuit power $P_c=1 W$ and the BS power ranges from 1 W to 12 W. It can be seen that the EE initially increases fast with respect to BS transmitted power and converges with slow growth, due to the total power constraints. This is because when BS power is relatively low, the optimal transmit power selection strategy uses all the available power at the BS. However, when total BS power is large enough, the transmit power selection strategy is limited to P^* regardless of total BS power. From Fig. 9, it is clearly shown that NOMA-SCP can achieve higher EE than NOMA-DC, NOMA-EQ and OFDMA

schemes.

In Fig. 10, the effectiveness of different power allocation schemes for multiplexed users is evaluated. Thus, we compare the proposed NOMA-SCP-UPA¹ scheme with NOMA-DC-DC and NOMA-EQ-FTPA, which is widely adopted in NOMA system for power allocation to users in the same subchannel [31], [19]. From Fig. 10, we can clearly see that by using NOMA-SCP-UPA scheme higher EE is achieved. Therefore, the proposed NOMA-SCP-UPA scheme outperforms both NOMA-DC-DC² and NOMA-EQ-FTPA³ for edge users in terms of EE. This clearly indicates the effectiveness of the proposed algorithm.

¹NOMA-SCP-UPA uses SCP approach to allocate power among different subchannels and the bisection search method to assign power between users grouped at the same subchannel.

²NOMA-DC-DC uses DC programming techniques to allocate power across subchannels as well as to determine the power allocation factor to allocate power between users grouped at the same subchannel.

³NOMA-EQ-FTPA uses equal power allocation across subchannels and FTPA to determine the power allocation factor between users on the same subchannel.

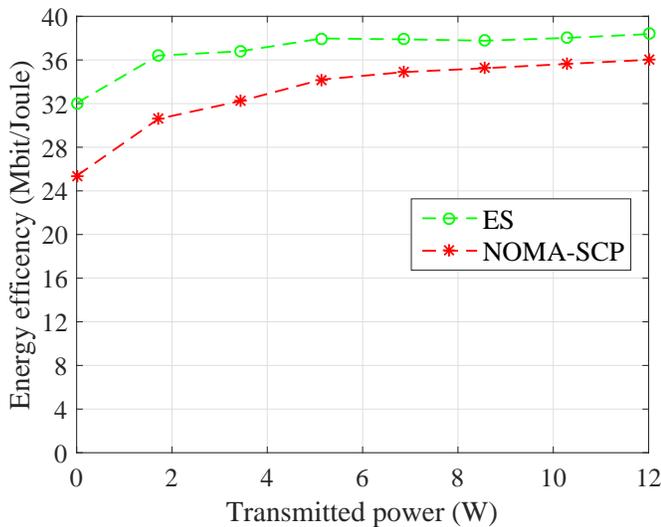


Fig. 11: Energy efficiency versus transmitted power

In order to get further insight on the performance of the proposed scheme, in Fig. 11, we compare the proposed scheme with the optimal solution through exhaustive search (i.e., ES) in terms of EE. It can be observed that the EE increases with the transmit power. It is also noticed that the proposed algorithm is capable of approaching the results of the exhaustive search. Recalling that the complexity of the proposed algorithm is much lower than the one of the exhaustive search, it is concluded that the proposed scheme achieves a good balance between complexity and performance.

VI. CONCLUSIONS

In this paper, we have investigated the downlink of MC-NOMA system where a single base station transmits a block of messages to multiple users. The focus has been on the maximization of the user with the lowest performance in terms of individual EE by optimizing subcarrier and power allocation. Since the optimization problem was non-convex, we formulated the subcarrier assignment and power allocation as a two stage-problem to reduce computational complexity. Then, a greedy subcarrier assignment scheme to assign two users on each subcarrier was proposed. Furthermore, for the power allocation, we transformed the non-convex problem into a simpler subtractive form using a fractional programming property. Thus, a suboptimal power allocation through the subchannels was obtained by iteratively solving the convex sub-problem using sequential convex programming. The provided simulation results have shown that the proposed resource optimization method achieves fast convergence and guarantees fairness. Consequently, the proposed resource allocation method is particularly promising, since remarkable gains are achieved compared to existing techniques, while it remains appropriate for the practical case.

APPENDIX A

PROOF OF THEOREM 1:

In complexity theory, to show a decision problem is NP-hard, we usually follow three steps [48] 1) choose a suit-

able known NP-complete decision problem A; 2) construct a polynomial time transformation from any instance of A to an instance of the required problem; 3) prove the two instances have the same objective value under the transformation. In the following section, we show that problems (14) is NP-hard.

Proof: The proof can be done into two cases for which $q_{k,n}=1$ and $q_{k,n} > 1$.

- 1) When $q_{k,n}=1$, (14) corresponds to an EE maximization problem with respect to joint subcarrier and power allocation for the conventional OFDMA system, which has been proved to be NP-hard in [47].
- 2) When $q_{k,n} > 1$, we prove that the problem is NP-hard even with known power allocation coefficients. In the following, we construct an instance of problem (14) with known power allocation coefficients. First, we will associate an instance of problem (14) as an equivalent to the Multiple Choice Knapsack problem (MCKP) problem, which is a well known NP-hard problem. We then consider an instance with $q_{k,n} = 2$. Thus, we prove a simplified version of the joint subcarrier and power allocation problem is reducible to the knapsack problem which is a well-known NP-hard problem.

Definition 1: Multiple Choice Knapsack problem (MCKP) [48]

Let's assume that there are N_1, N_2, \dots, N_S classes with each class i containing n_i items to be packed in a knapsack with capacity, P . Each item $j \in N_i$ has a profit $U_{i,j}$ and a weight $P_{i,j}$ and the problem is to assign some items to each class such that the profit is maximized without having the total weight exceeds P . It is generally considered that the profits, weights and the knapsack capacities take non-negative values.

Thus, we next show that problem in (14) is reduced to MCKP problem. Without loss of generality, we assume that each subcarrier is a knapsack and each item in the knapsack resembles a user to be packed in a knapsack of capacity, K_n . The profit of each item in the knapsack is the corresponding utility-function is $U_{i,j}$ and the required resource (weight) is $p_{i,j}$, while the Problem in (14) aims at choosing exactly K_n users (i.e., items) for each subcarrier (i.e., class) to maximize the EE, subject to the transmit power constraint, P_n . The EE maximization problem in (14) can be written in the following form:

$$\begin{aligned}
 \max_{Q,P} \min_{k=1,\dots,K} E_\eta(Q,P) &= \frac{R_{k,n}(Q,P)}{P_{k,n}^T(Q,P)} \\
 \text{s.t.} \quad C_3: \sum_{k=1}^{K_n} q_{k,n} P_{k,n} &\leq P_n, \quad \forall k \in K, \\
 C_4: \sum_{k=1}^K q_{k,n} &\leq K_n, \quad \forall n \in N, \\
 C_6: q_{k,n} &\in \{0, 1\}, \quad \forall k, n,
 \end{aligned} \tag{32}$$

Thus, (32) is NP-hard because it is categorized as a MCKP which is a generalization of the ordinary knapsack problem. Thus, as (32) is a special case of problem

(14), the general optimization problem (14) is an NP-hard problem.

APPENDIX B

PROOF OF THEOREM 2:

Proof: Without loss of generality, we assume that $R_k(P) \geq 0$ and $P_k(P) \geq 0$, where P and P^* denote any feasible power allocation and optimal power allocation policy, respectively, in (14). We also define e_k^* as the optimal EE for the original objective function in (14). Then, the EE is given by

$$\max_{P \in D} \min_{\mathcal{K}} \eta = \frac{R_k(P)}{P_k(P)}, \quad (33)$$

The equivalent parametric problem related to (33) is

$$\max_P \min_{\mathcal{K}} \{R_k(P) - \eta P_k(P)\}, \forall P \in D. \quad (34)$$

The following *Lemma 1* is introduced to show the relation between (33) and (34).

Lemma 1: if P^* is the optimal solution of (33) with corresponding parameter introduced by $\eta^* = \frac{R_k(P^*)}{P_k(P^*)}$, then P^* is also the optimal solution of (34). Since P^* maximizes $\{R_k(P) - e_k^* P_k(P)\}, \forall P \in D$, we have

$$R_k(P) - e_k^* P_k(P^*) \leq R_k(P^*) - \eta_k^* P_k(P^*), \forall P \in D. \quad (35)$$

From the definition of η^* , we have

$$\{R_k(P^*) - \eta^* P_k(P^*)\}, \forall P \in D. \quad (36)$$

Combining (36) and (35), we obtain

$$\{R_k(P) - \eta P_k(P)\} \leq \{R_k(P^*) - \eta P_k(P^*)\} = 0. \quad (37)$$

From this

$$R_k(P) - \eta P_k(P^*) \leq 0 \text{ or } \eta^* \geq \frac{R_k(P)}{P_k(P)}. \quad (38)$$

This indicates that

$$\eta^* = \frac{R_k(P)}{P_k(P)}, \text{ is the maximum of } \frac{R_k(P)}{P_k(P)}, \forall P \in D. \quad (39)$$

In other words P^* is the optimal solution of (31). Therefore, the optimal resource allocation for the equivalent objective function is also the optimal resource allocation for the original objective function. This completes the proof. ■

APPENDIX C

PROOF OF THEOREM 3:

Proof: Let's start with an initial interval $[\eta_{\min}, \eta_{\max}]$, for which

$$\eta = \frac{(\eta_{\min} + \eta_{\max})}{2} \text{ and } d = F(\eta_{\min}) \cdot F(\eta_{\max}). \quad (40)$$

- If $d < 0$, let $\eta_{\max} = \eta$ and $\eta_{\min} = \eta_{\min}$.
- If $d > 0$, let $\eta_{\min} = \eta$ and $\eta_{\max} = \eta_{\max}$.
- If $d = 0$, then η becomes the solution with the required accuracy, ϵ .

For either of the two cases, the new interval is one half of the width of the original. This new interval is reformed as $[\eta_{\min}, \eta_{\max}]$ and the procedure is repeated again. Over the

j -th iterations, it follows that

- The first interval is $[\eta_{\min}^0, \eta_{\max}^0]$ and $\eta^0 = \frac{(\eta_{\min}^0 + \eta_{\max}^0)}{2}$
 - The Second interval is $[\eta_{\min}^1, \eta_{\max}^1]$ and $\eta^1 = \frac{(\eta_{\min}^1 + \eta_{\max}^1)}{2}$
 - The j -th interval is $[\eta_{\min}^j, \eta_{\max}^j]$ and $\eta^j = \frac{(\eta_{\min}^j + \eta_{\max}^j)}{2}$
- where $\eta_{\min}^j = \eta^{j-1}$ and $\eta_{\max}^j = \eta_{\max}^{j-1}$ or $\eta_{\min}^j = \eta_{\min}^{j-1}$ and $\eta_{\max}^j = \eta_{\max}^{j-1}$. From this we can observe that

- The sequence $\{\eta_{\min}^j\}_{j=0}^{\infty}$ is increasing sequence and bounded above by η_{\max} .
- The sequence $\{\eta_{\max}^j\}_{j=0}^{\infty}$ is decreasing sequence and bounded below by η_{\min} .
- and the approximated sequence of η^j 's generated by the bisection is found on $\eta_{\min}^j \leq \eta^j \leq \eta_{\max}^j$, for all j . Moreover, the function $F(\eta)$ is strictly decreasing in η [36], [37]. In addition, $F(\eta)$ is negative for $\eta \rightarrow +\infty$ and positive for $\eta \rightarrow -\infty$. This satisfied $F(\eta_{\min}^j) \cdot F(\eta_{\max}^j) < 0$.

Furthermore, let us define the approximation at η^j after the j -th iteration as the midpoint

$$\eta^j = \frac{(\eta_{\min}^j + \eta_{\max}^j)}{2}. \quad (41)$$

Since the actual solution $F(\eta^*)=0$ satisfies $\eta \in \frac{\eta_{\max}^j - \eta_{\min}^j}{2}$, we have

$$|\eta^j - \eta^*| < \frac{1}{2} \left| \frac{\eta_{\max}^j - \eta_{\min}^j}{2} \right|. \quad (42)$$

Since the length of the current search interval gets divided in half in each iteration, we have

$$|e^j| = |\eta^j - \eta^*| \leq \left(\frac{1}{2}\right)^j \left| \frac{\eta_{\max}^j - \eta_{\min}^j}{2} \right|. \quad (43)$$

From this, we have $\lim_{j \rightarrow \infty} e^j = 0$. For $\lim_{j \rightarrow \infty} \frac{1}{2^j} = 0$, we obtain $\eta^j = \eta^*$, which proves the global convergence of the bisection method. We interpret this behavior as linear convergence.

Moreover, let the ϵ be the relative accuracy of the root, then to estimate the number of iteration j to achieve the accuracy is given by

$$\frac{|\eta^j - \eta^*|}{|\eta^*|} \leq \epsilon. \quad (44)$$

Let's assume that the root lies in $[\eta_{\min}, \eta_{\max}]$ where $\eta_{\max} > \eta_{\min} > 0$. Clearly, $|\eta^*| \geq \eta_{\min}$ and hence the above relation is true if

$$\frac{|\eta^j - \eta^*|}{\eta^*} \leq \epsilon, \quad (45)$$

which is true if

$$\frac{\eta_{\max} - \eta_{\min}}{(2^{j+1})\eta^*} \leq \epsilon. \quad (46)$$

Solving this we can find the minimum number of iterations needed to obtain the desired accuracy. Now, it can be derived that

$$|e^{j+1}| = |\eta^{j+1} - \eta^*| \leq \frac{1}{2} (\eta_{\max}^{j+1} - \eta_{\min}^{j+1}) = \frac{1}{2} (\frac{\eta_{\max} - \eta_{\min}}{2}) \quad (47)$$

and

$$|e^j| = |\eta^j - \eta^*| \leq \frac{1}{2}(\eta_{\max}^j - \eta_{\min}^j). \quad (48)$$

Thus, we find $|e_{j+1}| \approx \frac{1}{2} |e_j|$. Therefore, the proposed bisection method in order to determine η^* converges linearly. This completes the proof. ■

APPENDIX D PROOF OF THEOREM 4:

As P^t is feasible to (31), it follows that

$$E^t = \min_k (f_k(P^{t+1}) - g_k(P^{t+1})) \geq \min_k (f_k(P^t) - [g_k(P^t) + \nabla g_k^T(P^t)(P^{t+1} - P^t)]) \geq \min_k (f_k(P^t) - g_k(P^t)) = E^{t+1} \quad (49)$$

The next solution P^{t+1} is always better than the previous solution P^t . That is $\min(f_k(P^t) - g_k(P^t))$ monotonically decreases when the iteration t increases. With successive iterations of the algorithm, the value of $E^{(t)} = \min(f_k(P^t) - g_k(P^t))$ decreases. Moreover, for every $E^{(t)}$ the power vector P that maximize $f_k(P) - [g_k(P^t) + \nabla g_k^T(P^t)(P - P^t)]$ is found. Thus, iteration process terminates after a finite iteration at $\min(f_k(P^t) - g_k(P^t)) \leq \epsilon$ (no solution progress) with some threshold $\epsilon \geq 0$. Hence, the iterative power control algorithm converges in a finite step. Furthermore, since the constraint set is compact, by Cauchy Theorem the sequence P^t of improved solution always converges [42]. From this, we can conclude that Algorithm 3 is guaranteed to converge.

b) Proof of optimal transmit power converges to a stationary point Consider Proof of algorithm convergence, we now prove problem (28) in algorithm 3 for optimal transmit power converges to a stationary point under an additional assumption $f_k(P)$ and $g_k(P)$ defined in $f_k(P) - g_k(P)$ are continuous and differentiable over a given constraint sets. Since $-g_k(P)$ is approximate by its convex function as

$$g_k(P^t) + \nabla g_k^T(P^t)(P - P^t) \quad (50)$$

The objective function is rewritten as

$$Q_k(P) = f_k(P^t) - [g_k(P^t) + \nabla g_k^T(P^t)(P - P^t)] \quad (51)$$

In the limit all inequalities in (36) become equality. In other words, P^t and P^{t+1} are optimal point of the objective function over the defined constraint sets [35]. Hence, $\hat{P}^t = P^{t+1}$ and

$$P^{t+1} = \arg \max_{P \in \{C^1, C^2, C^4\}} \min_{\mathcal{K}} Q_k(P) \quad (52)$$

Furthermore, according to optimality condition [35], we have

$$\min_{\mathcal{K}} \nabla Q_k^T(P^t)(P - P^t) = \min_{\mathcal{K}} \{\nabla Q_k(P^{t+1})(P - P^{t+1})\} \leq 0 \quad (53)$$

which can be equivalent to [40]

$$\min_{\mathcal{K}} \{\nabla f_k(P^t) + \nabla g_k^T(P^t)(P - P^t)\} \leq 0. \quad (54)$$

Thus, P^t is the stationary point to (31) i.e. (20). This completes the proof.

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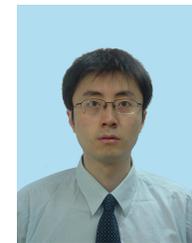
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